

Work & Power

Work is done when energy changes

$$W = \Delta E$$

A change in E_p or E_k

$W = \Delta E$ => the work/ energy theorem

Units of work are joules

How much work is done in lifting a 4.0 kg cat carcass to height 2.0 m?

$$\begin{aligned} W &= \Delta E_p \\ &= E_{pf} - E_{pi} \\ &= mgh_f - mgh_i = 4(9.8)2 - 4(9.8)0 = 78.4 \text{ J} \end{aligned}$$

Some random non-physics loser kid of mass 60 kg rides their bike at 6.0 m/s and accelerates to 10 m/s, how much work was done before they got hit by a bus?

$$\begin{aligned} W &= \Delta E_k \\ &= E_{kf} - E_{ki} \\ &= \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 = \frac{1}{2}(60)10^2 - \frac{1}{2}(60)6^2 \\ &= 3000 - 1080 = 1920 \text{ J} \end{aligned}$$

os 30) 3
(cos 30) 100

A cat at rest with mass 5.0 kg is kicked and seen moving at 4.0 m/s and height 3.0 m, What work was done on the cat?

$$\begin{aligned} W &= \Delta E_k + \Delta E_p \\ W &= E_{kf} - E_{ki} + E_{pf} - E_{pi} \\ &= \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 + mgh_f - mgh_i \\ &= 40 - 0 + 147 - 0 = 187 \text{ J} \end{aligned}$$

Work is done when a force moves an object across a distance

$$W = F \cdot d$$



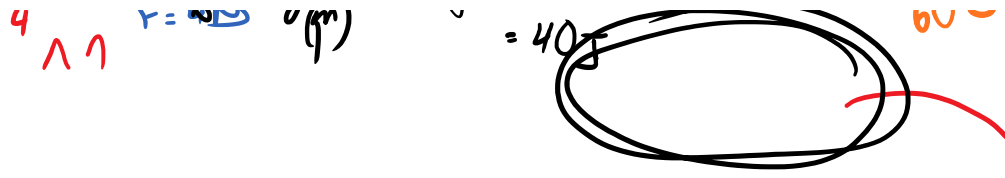
Force and distance MUST be parallel AND the force must stay constant

Find the work done!

$$\begin{aligned} W &= F \cdot d \\ &= 86.6 (20) \\ &= 1730 \text{ J} \end{aligned}$$

A cat is pushed 10m along the floor using a force of 4.0 N, what work is done?

$$4 \text{ N} \quad F = 4 \text{ N} \quad d = 10 \text{ m} \quad W = Fd = 40 \text{ J} \quad 60 \text{ J}$$



A shovel is pushed using a force of 100 N along the handle as shown at 30° to the ground, for 3.0 m to move snow. What work is done?

$$A = \frac{1}{2} l w$$

$$A = l w$$



GRAPHS:

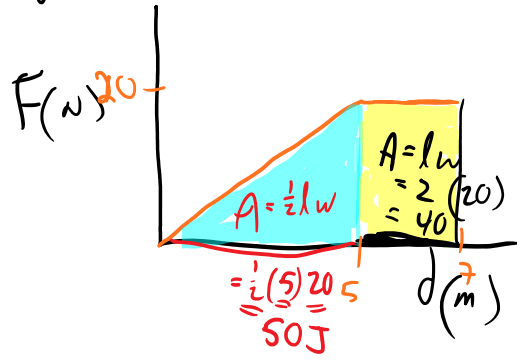
Force is not constant

Work = AREA of The graph

Force vs distance

$$\frac{50 + 40}{2} = 45$$

$$45 \times 2 = 90 \text{ J}$$



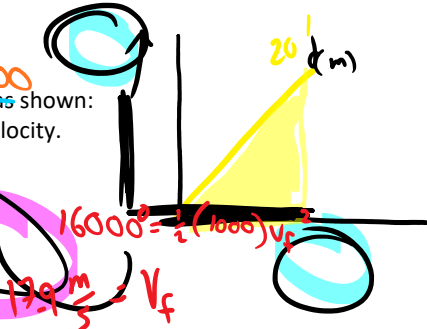
$$\text{Area} = \text{Work}$$

$$\frac{b \cdot h}{2} = \frac{20 \cdot 16000}{2} = 160000$$

A car is accelerated from rest with a force as shown: If the car has mass 1000 kg find the final velocity.

$$W = \Delta E_k + \Delta E_p$$

$$W = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_0^2$$



$$0 = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_0^2$$

$$16000 = \frac{1}{2} (1000) v_f^2$$

$$32000 = 1000 v_f^2$$

$$v_f^2 = 32$$

$$v_f = 5.66 \text{ m/s}$$

AJ's mass 48kg and jumps up on a desk of height 1.5 m in 2.0 sec find the work done!!!!!!

Area F vs d

$$W = \Delta E_p$$

$$W = mgh_f - mgh_0$$

$$= 48(9.8)2 = 940.8 \text{ J}$$

$$W = \Delta E_k$$

look for vertical motion changing

$$3(9.8) \left[\frac{4}{2} \right]$$

$$\Rightarrow 118 \text{ J}$$

$$\frac{mgh}{t} = \frac{84(9.8)(1.5)}{2} = 615 \text{ W}$$

power required for this!!!

power required for this!!!

$$= 615 \text{ W}$$

A cat of mass 8.0 kg is accelerated from 5.0 m/s according to the graph, find the final velocity

A 1000 kg car accelerates from rest

To a velocity of 12 m/s in 4.0 s, find the power of the engine!!!!

$$\frac{12}{4} = 3$$

x

POWER: Work done per unit of time <= how fast you work

$$P = \frac{W}{t}$$

A cat of mass 10 kg at rest is kicked slowly until a speed of 6.0 m/s is reached in 18 seconds, find the power needed to do this.

$$P = \frac{W}{t}$$

$$W = \Delta E_k$$

$$\begin{aligned} W &= E_{kf} - E_{k0} \\ &= \frac{1}{2} m v_f^2 - \frac{1}{2} m v_0^2 \\ &= \frac{1}{2} (10) 6^2 = 180 \end{aligned}$$

$$P = \frac{180}{18} = 10 \text{ W}$$

Watts ← unit of power

Finish + sheets or cas in your house

$$\begin{aligned} v_f &= 12 \\ v_0 &= 0 \\ t &= 4 \\ P &= \frac{1}{2} (1000) 12^2 = 18000 \text{ W} \end{aligned}$$

ENERGY: energy is the ability to change some conditions in the universe

Units are Joules, same as work

2 main categories for energy

POTENTIAL ENERGY (E_p)

Energy stored, waiting to cause a change

Gravitational $E_p = mg\Delta h$

KINETIC ENERGY (E_k)

energy in use causing a change

energy in a moving mass $E_k = \frac{1}{2}mv^2$

Energy stored, waiting to cause a change

Energy in use causing a change

$$\text{Gravitational } E_p = mg\Delta h$$

$$\text{energy in a moving mass } E_k = 1/2mv^2$$

$$\text{Elastic } E_p = 1/2 kx^2$$

Heat energy in moving molecules

$$E_h = mc\Delta T$$

$$\text{Energy stored in mass } E = mc^2$$

m = mass in kilograms

g = gravitational field (9.8 m/s² on Earth)

Δh = change in height from low point

V = velocity in m/s

K = spring constant in N/m

X = extension or compression in meters

C = speed of light (3.00 x 10⁸ m/s)

ΔT = change in temperature (°C)

The WORK/ENERGY THEOREM states work done on an object changes its energy

$$W = \Delta E$$

Example 1: a spring with constant 25 N/m is stretched from 15 cm to 20 cm, what is the work done on the spring?

$$W = \Delta E$$

$$W = E_{pf} - E_{po}$$

$$W = 1/2 kx^2 - 0$$

$$W = 1/2 (25)(0.20 - 0.15)^2$$

$$W = 0.0313 \text{ J}$$

Example 2: 90 J of work are done accelerating a 10 kg cat from 3.0 m/s, What is its final velocity?

$$W = \Delta E$$

$$W = E_{kf} - E_{ko}$$

$$W = 1/2 mv_f^2 - 1/2 mv_o^2$$

$$90 = 1/2 (10)(v_f^2) - 1/2(10)(3^2)$$

$$90 = 5v_f^2 - 45$$

$$135 = 5v_f^2$$

$$27 = v_f^2$$

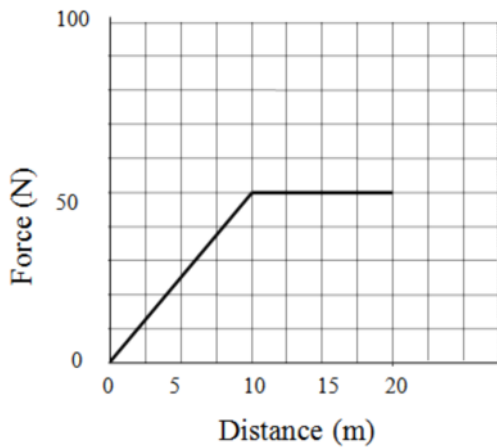
$$v_f = 5.2 \text{ m/s}$$

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The work / energy theorem states that the work done on an object is equal to the change in energy it receives!

A cat on fire has mass 3.0 kg is lifted from 2.0 m above a spike to 3.5 m above the same



Thursday ← Lab

POWER ≤ the rate at which work is done

$$P = W / t$$

Power is measured in units of J/s which is the WATT.
For large amounts of power a larger unit

Known as horsepower was used,

1.0 horsepower (or 1.0 hp) = 750 W

A 100W light bulb operates for 1.0 hour. How much work was done?

Greta pulls a wagon 10m using a force of 300N along the handle which is inclined at 60° to the horizontal for 20 seconds, what power does Greta produce?