

Entropy

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Entropy

disordered transmission of energy

Entropy is the random or disordered motion of molecules. The absolute entropy of a particular object is not measurable, only the change in entropy can be calculated.

In formula change in entropy is represented by ΔS and has units of Joules / Kelvin (or cal / K).

** $\Delta S = Q / T$

Note that Q may be calculated in any thermodynamic manner ($Q = mc\Delta T$, mL, or $\Delta U = Q + W$)

Using eqn. ** is simple if T is constant. But in cases where $\Delta T \neq 0$ the calculation can still be performed using average temperatures if ΔT is small

Example 1 change in entropy during a phase change:

A 1.25 kg mass of lead at 327 °C is allowed to melt, calculate the change in entropy.

- $\Delta S = \frac{Q}{T} \leftarrow Q = mL_f = 1.25 \times 0.25 \times 10^5 = 3.125 \times 10^4 \text{ J}$
 $T \leftarrow T = 327 + 273 = 600 \text{ K}$
- $\Delta S = 52 \text{ J / K}$

$\Delta E = 0 = mc\Delta T_{30} + mc\Delta T_{20}$
 $0 = .4(4186)(T_f - 30) + .3(4186)(T_f - 20)$
 $T_f = 25.7^\circ\text{C}$

Example 2 change in entropy involving temperature change

A 400 gram sample of water at 30 °C is mixed with a 300 gram sample at 20 °C. Calculate the change in entropy of the 400 g sample, the 300 g sample and the entire system.

First calculate the final temperature of the entire system:

- $\Delta Q = 0 = mc\Delta T_{30} + mc\Delta T_{20}$
 $0 = .400(4186)(T_f - 30) + .300(4186)(T_f - 20)$
 $0 = 1674.4T_f - 50232 + 1255.8T_f - 25116$
 $0 = 2930.2T_f - 75348$
 $T_f = 25.7^\circ\text{C} = 298.7 \text{ K}$

Using the final temperature determine the change in entropy of each sample in the experiment:

30 → 25.7 20 → 25.7

- $\Delta S = \Delta S_{\text{hot}} + \Delta S_{\text{cold}}$
- $\Delta S = \frac{mc\Delta T_{\text{hot}}}{T_{\text{avehot}}} + \frac{mc\Delta T_{\text{cold}}}{T_{\text{avecold}}} = \frac{0.400(4186)(25.7 - 30)}{[(25.7 + 30)/2] + 273} + \frac{0.300(4186)(25.7 - 20)}{[(25.7 + 20)/2] + 273} = \frac{-7199.92}{300.85} + \frac{7158.06}{295.85}$
- $\Delta S = -23.9 + 24.2 = 0.30 \text{ J / K}$

Note that while the hot body has ΔS negative the cold body has a larger ΔS positive resulting a positive

existence of Hawking radn in reference to blackholes & Thermodynamics

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