

Air Columns

Monday, May 17, 2010 9:04 AM

Vibrating air columns consist of two types:

1) open at both ends => toilet paper roll, trumpet,

2) open at one end => can of soup, glass bottle

Speed of sound in air at 25°C and 1 atm pressure = 343 m/s

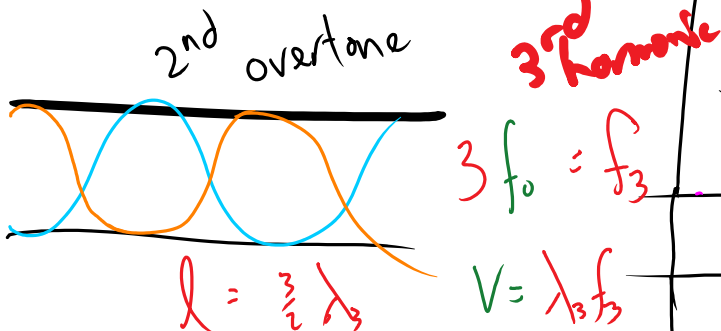
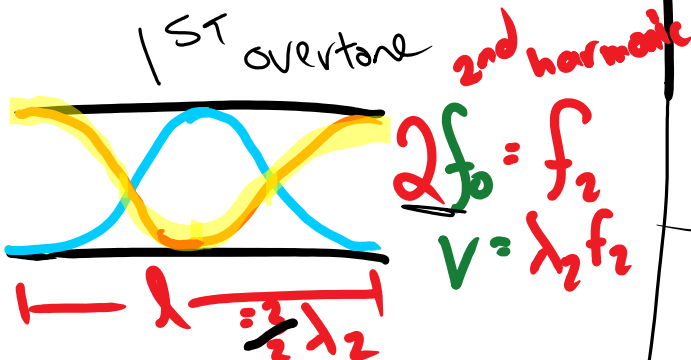
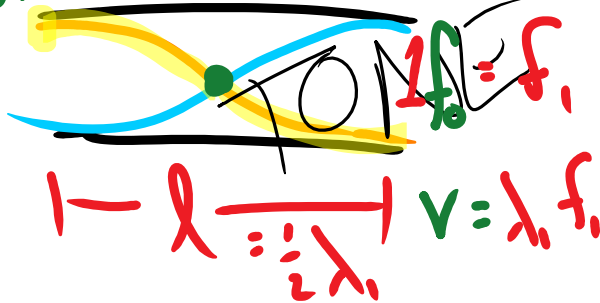
At an open end the air is free to oscillate forth and back. The result is an anti-node at every open end.

$$V_{\text{sound}} = 340 \frac{\text{m}}{\text{s}}$$

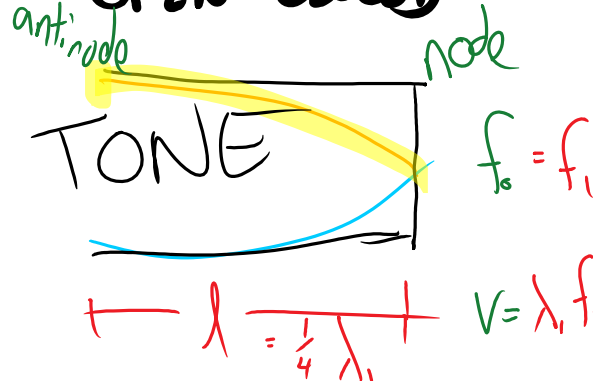
At a closed end the air is not free to oscillate and a node occurs.

Only certain wavelengths may exist in air columns based on the length of the air column.

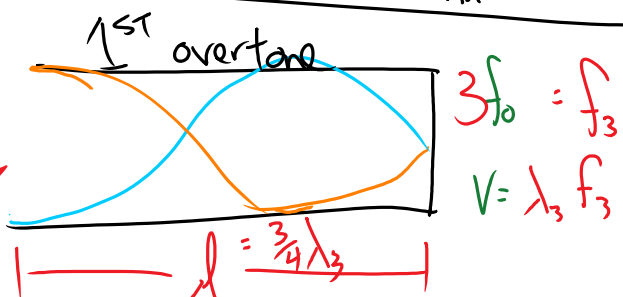
OPEN - OPEN
antinode node antinode



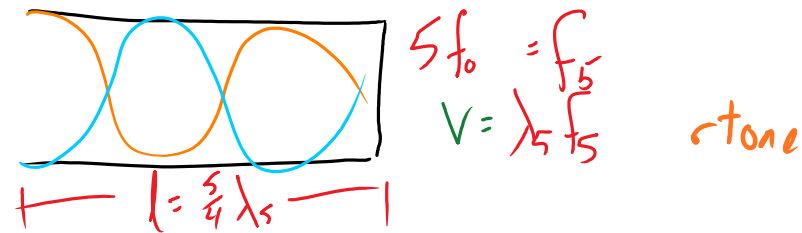
OPEN - CLOSED

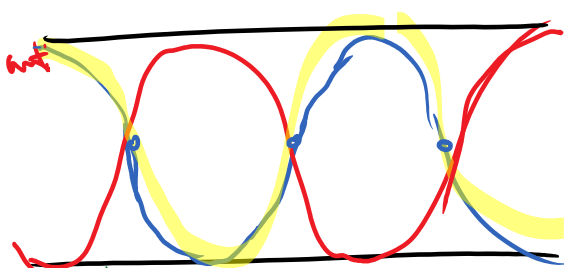


No f_2
No even harmonics



f_4 does not exist





3rd harmonic $3f_0 = f_3$

$$l = \frac{3}{2} \lambda_3$$

2nd overtone

$$l = \frac{3}{2} \lambda_3$$

$$v = \lambda_3 f_3 = \frac{3}{2} l f_3$$

2nd overtone

general form

$$f_n = n f_0$$

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$$\lambda_n = \frac{n}{2} \lambda_1$$

$$l = \frac{n}{2} \lambda_n$$

As long v stays constant

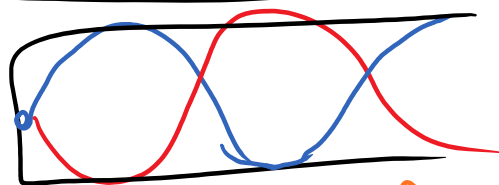
$$v = \lambda f$$

$$v = \lambda_0 f_0 = \lambda_3 f_3$$

A-F

$$l = \frac{5}{4} \lambda_5$$

anti



5th harm = $5f_0$

$$l = \frac{5}{4} \lambda_5$$

2nd overtone

general form

$$f_n = n f_0$$

$$n \neq 2, 4, 6, \dots$$

$$\lambda_n = \frac{n}{4} \lambda_1$$

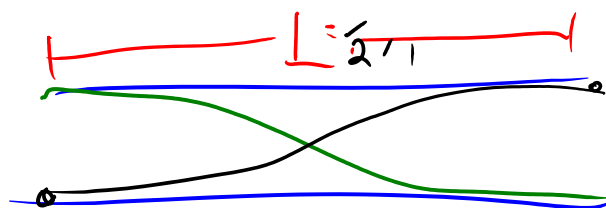
$$l = \frac{n}{4} \lambda_n$$

$$\frac{f_0}{f_3} = \frac{\lambda_3}{\lambda_0}$$

$$f_1 = 264 \text{ Hz}$$

$$v = \lambda_1 f_1$$

$$\frac{343}{264} = \lambda_1 = 1.3$$



$$L = \frac{1}{2} 1.3 \text{ m}$$

$$= 0.65 \text{ m}$$

$$f_0 = 264 \text{ Hz}$$

$$L = \frac{1}{2} (1.3) = 0.65 \text{ m}$$

$$\frac{343}{264} \lambda_0 = 1.299 \text{ m}$$

Do A \rightarrow F